# Register Transfer Methodology I

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#### 1. Introduction

- How to realize an algorithm in hardware?
- Two characteristics of an algorithm:
  - Use of variables (symbolic memory location) e.g., n = n + 1 in  $\dot{C}$
  - Sequential execution (execution order is important)

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- "Dataflow" implementation in VHDL
  - Convert the algorithm in to combinational circuit
  - No memory elements
  - The sequence is embedded into the "flow of data"

#### Outline

- 1. Introduction
- 2. Overview of FSMD
- 3. FSMD design of a repetitive-addition multiplier
- 4. Alternative design of a repetitiveaddition multiplier
- 5. Timing and performance analysis of **FSMD**
- 6. Sequential add-and-shift multiplier

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- · E.g., an algorithm:
  - Summate 4 number
  - Divide the result by 8
  - Round the result
- Pseudocode

```
size = 4
sum = 0;
for i in (0 to size-1) do {
  sum = sum + a(i);
q = sum / 8;
r = sum rem 8;
if (r > 3) {
   q = q+1;
outp = q;
```

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VHDL code

```
sum <= 0;
sum0 <= a(0);
sum1 <= sum0 + a(1);
sum2 \le sum1 + a(2);
sum3 \le sum2 + a(3);
q <= "000" & sum3(8 downto 3);
r <= "00000" & sum3(2 downto 0);
outp \leq q + 1 when (r > 3) else
        q;
```

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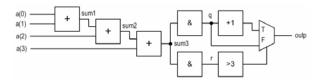
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#### · Block diagram



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- Problems with dataflow implementation:
  - Can only be applied to trivial algorithm
  - Not flexible
    - Can we just share one adder in a timemultiplexing fashion to save hardware resources
    - What happen if input size is not fixed (i.e., size is determined by an external input)

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# Register Transfer Methodology

- · Realized algorithm in hardware
- Use register to store intermediate data and imitate variable
- Use a datapath to realize all register operations
- Use a control path (FSM) to specify the order of register operation

- The system is specified as sequence of data manipulation/transfer among registers
- Realized by FSM with a datapath (FSMD)

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2. Overview of FSMD

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# Basic RT operation

• Basic form:

$$\mathbf{r}_{\text{dest}} \leftarrow f(\mathbf{r}_{\text{src1}}, \mathbf{r}_{\text{src2}}, \dots, \mathbf{r}_{\text{srcn}})$$

- · Interpretation:
  - At the rising edge of the clock, the output of registers  $r_{\rm src1}$   $r_{\rm src2}$  etc are available
  - The output are passed to a combinational circuit that performs f()
  - At the next rising edge of the clock, the result is stored into  $\rm r_{\rm dest}$

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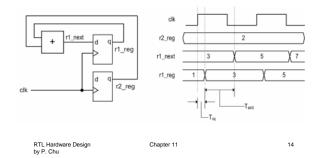
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 $\begin{array}{ll} \bullet \text{ E.g.,} & r \leftarrow 1 \\ & r \leftarrow r \\ & r0 \leftarrow r1 \\ & n \leftarrow n-1 \\ & y \leftarrow a \oplus b \oplus c \oplus d \\ & s \leftarrow a^2 + b^2 \end{array}$ 

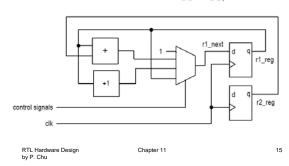
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Implementation example

$$r1 \leftarrow r1+r2$$



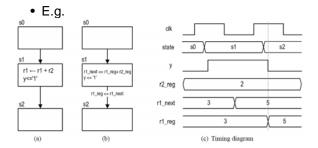
 $\begin{array}{ll} \bullet \text{ Multiple RT operations} & \begin{array}{ll} r1 \leftarrow 1; \\ r1 \leftarrow r1 + r2; \\ r1 \leftarrow r1 + 1; \\ r1 \leftarrow r1; \end{array}$ 



FSM as control path

- FSM is a good to control RT operation
  - State transition is on clock-by-clock basis
  - FSM can enforce order of execution
  - FSM allows branches on execution sequence
- Normally represented in an extended ASM chart known as ASMD (ASM with datapath) chart

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• Note: new value of r1 is only available when the FSM exits s1state

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Basic Block Diagram of FSMD

data path

routing network functional units routing network registers

command output status signals

control path

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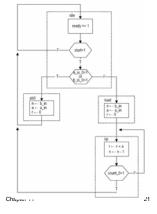
# 3. FSMD design example: Repetitive addition multiplier

- Basic algorithm: 7\*5 = 7+7+7+7
- Pseudo code

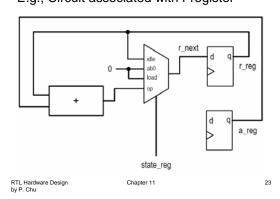
```
if (a_in=0 or b_in=0) then {
    r = 0;}
else {
    a = a_in;
    n = b_in;
    r = 0;
    while (n != 0) {
        r = r + a;
        n = n-1;}
}
return(r)
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```

- Input:
  - a\_in, b\_in: 8-bit unsigned
  - clk, reset
  - start: command
- · Output:
  - r: 16-bit unsigned
  - ready: status
- ASMD chart
  - Default RT operation: keep the previous value
  - Note the parallel execution in op state

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# • E.g., Circuit associated with r register



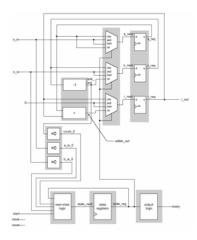
#### ASMD-friendly code

```
if (a_in=0 \text{ or } b_in=0) then {
               r = 0;}
            else {
               a = a_in;
               n = b_in;
               r = 0;
               r = r + a;
    op:
               n = n-1;
               if (n = 0) then {
                   goto stop;}
               else {
                  goto op;}
           }
    stop: return(r);
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```

#### · Construction of the data path

- List all RT operations
- Group RT operation according to the destination register
- Add combinational circuit/mux
- Add status circuits
- E.g RT operations with the r register:
  - $\ r \leftarrow r \ (in \ the \ idle \ state)$
  - $\ r \leftarrow 0 \ (in \ the \ load \ and \ op \ states)$
  - $r \leftarrow r + b (in the op state)$
  - RT operations with the n register:
    - $n \leftarrow n \text{ (in the idle state)}$
    - n  $\leftarrow$  a\_in (in the load and ab0 states)
    - $\ n \leftarrow n \ \ 1 \ (in \ the \ op \ state)$
  - RT operations with the b register:
    - b ← b (in the idle and op states)

RTL Hardware by P. Chu  $-b \leftarrow b_{in}$  (in the load and ab0 states)



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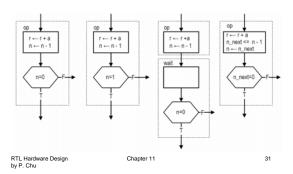
```
    VHDL code: follow the block diagram

                                                                                  -- control path: state register
                                                                                   process (clk, reset)
   library ieee;
                                                                                   begin
  use ieee.std_logic_1164.all;
                                                                                      if reset='1' then
  use ieee.numeric_std.all;
                                                                                           state_reg <= idle;
                                                                                        elsif (clk'event and clk='1') then
   entity seq_mult is
                                                                                          state_reg <= state_next;
      port (
                                                                                        end if;
         clk, reset: in std_logic;
                                                                                   end process;
         start: in std_logic;
         a_in, b_in: in std_logic_vector(7 downto 0);
         ready: out std_logic;
         r: out std_logic_vector(15 downto 0)
         );
   end seq_mult;
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                                                                               RTL Hardware Design by P. Chu
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                                                                                                        Chapter 11
           - control path: next-state/output logic
                                                                                   -- control path: output logic
ready <= '1' when state_reg=idle else '0';</pre>
          process(state_reg, start, a_is_0, b_is_0, count_0
          begin
            - data path: data register
                                                                                    process (clk, reset)
                                                                                    begin
                                                                                        if reset='1' then
                     state_next <= load;
end if;
                                                                                           a_reg <= (others=>,0,);
                                                                                           n_reg <= (others=>'0');
               end if;
clse
    state_next <= idle;
end if;
when ab0 =>
    state_next <= idle;
when load =>
                                                                                            r_reg <= (others => '0');
                                                                                        elsif (clk'event and clk='1') then
                                                                                           a_reg <= a_next;
                                                                                            n_reg <= n_next;
                  state_next <= op;
                                                                                            r_reg <= r_next;
               when op =>
  if count_0='1' then
    state_next <= idle;</pre>
                                                                                        end if;
                                                                                    end process;
                  else

state_next <= op;

end if;
             end case:
                                                                               RTL Hardware Design
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                                                                                                        Chapter 11
   RTL Hardw end process;
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             -- data path: routing multiplexer
             process (state_reg , a_reg , n_reg , r_reg ,
                      a_in,b_in,adder_out,sub_out)
                                                                              -- data path: functional units
                case state_reg is
                                                                              adder_out <= ("00000000" & a_reg) + r_reg;
                    when idle =>
                                                                              sub_out <= n_reg - 1;
                      a_next <= a_reg;
                       n_next <= n_reg;
                    r_next <= r_reg;
when ab0 =>
                                                                               – data path: status
                                                                             a_is_0 <= '1' when a_in="00000000" else '0';
                       a_next <= unsigned(a_in);
                                                                              b_is_0 <= '1' when b_in="00000000" else '0';
                       n_next <= unsigned(b_in);
r_next <= (others=>'0');
                                                                              count_0 <= '1' when n_next="00000000" else '0';
                    when load =>
                                                                              -- data path: output
                       a_next <= unsigned(a_in);
                       n_next <= unsigned(b_in);
                                                                              r <= std_logic_vector(r_reg);
                       r_next <= (others=>'0');
                    when op =>
                       a_next <= a_reg;
                        n_next <= sub_out;
                       r_next <= adder_out;
                   end case;
                                                          29
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                                                                                                                                       30
           end process;
```

- · Use of register in decision box
  - Register is updated when the FSM exits current state
  - How to represent count\_0='1' using register?



- Other VHDL coding styles:
  - Various code segments can be combined
  - Should always separate registers from combinational logic
  - May be a good idea to isolate the main functional units

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#### • E.g., 2-segment code

```
state and data register
 process (clk, reset)
 begin
     if reset='1' then
        state_reg <= idle;
        a_reg <= (others=>'0');
        n_reg <= (others=>'0');
        r_reg <= (others=>'0');
     elsif (clk'event and clk='1') then
        state_reg <= state_next;
        a_reg <= a_next;
        n_reg <= n_next;
        r_reg <= r_next;
    end if;
 end process;
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```

```
combinational circuit
process(start,state_reg,a_reg,n_reg,r_reg,
        a_in,b_in,n_next)
begin
   .
-- default value
   a_next <= a_reg;
   n_next <= n_reg;
   r_next <= r_reg;
  ready <='0';
case state_reg is
      when idle =>
         if start='1' then
            if (a_in="00000000" or b_in="00000000") then
                state_next <= ab0;
             else
                state_next <= load;
             end if;
               state_next <= idle;
         end if;
         ready <= '1';
```

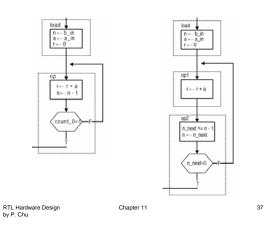
```
when ab0 =>
             a_next <= unsigned(a_in);
n_next <= unsigned(b_in);
             r_next <= (others=>'0');
             state_next <= idle;
         when load =>
             a_next <= unsigned(a_in);
n_next <= unsigned(b_in);
r_next <= (others=>'0');
             state_next <= op;
ready <='0';
         when op =>
             n_next <= n_reg - 1;
r_next <= ("00000000" & a_reg) + r_reg;
if (n_next="00000000") then
                 state_next <= idle;
              else
             state_next <= op;
end if;</pre>
              ready <= '0';
    end case:
end process;
r <= std_logic_vector(r_reg);
```

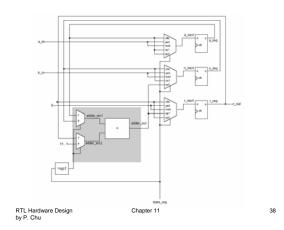
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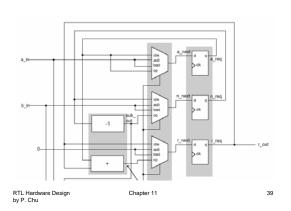
## 4. Alternative design of a repetitiveaddition multiplier

- Resource sharing
  - Hardware can be shared in a timemultiplexing fashion
  - Assign the operation in different states
  - Most complex circuits in the FSMD design is normally the functional units of the datapath
- Sharing in repetitive addition multiplier
  - Addition and decrementing
  - The same adder can be used in 2 states

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```
when op1 =>
    r_next <= adder_out;
    state_next <= op2;
when op2 =>
    n_next <= adder_out(WIDTH-1 downto 0);
    if (n_next="00000000") then
        state_next <= idle;
    clse
        state_next <= op1;
    end if;</pre>
```

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```
-- data path input routing and functional units

process(state_reg,r_reg, a_reg, n_reg)

begin

if (state_reg=op1) then

adder_src1 <= r_reg;

adder_src2 <= "00000000" & a_reg;

else -- for op2 state

adder_src1 <= "00000000" & n_reg;

adder_src2 <= (others=>'1');

end if;

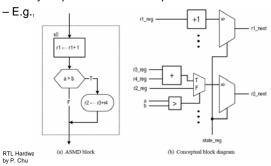
end process;

adder_out <= adder_src1 + adder_src2;
```

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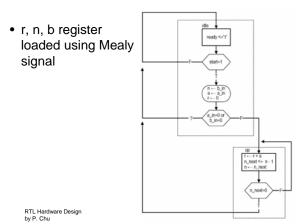
### • Mealy-controlled operation

- Control signals is edge-sensitive
- Mealy output is faster and requires fewer states



- Mealy control signal for multiplier
  - load and ab0 states perform no computation
  - Mealy control can be used to eliminate ab0 and load states

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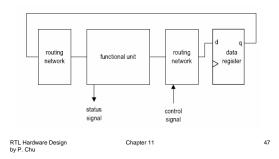
```
case state_reg is
  when idle =>
    if start='1' then
       a_next <= unsigned(a_in);
       n_next <= unsigned(b_in);
       r_next <= (others=>'0');
    if a_in="00000000" or b_in="00000000" then
            state_next <= idle;
    else
            state_next <= op;
    end if;
    clse
        state_next <= idle;
    end if;
    ready <='1';
    when op =>
       n_next <= n_reg - 1;
       r_next <= ("00000000" & a_reg) + r_reg;
    if (n_next="0000000") then
        state_next <= idle;
    else
        state_next <= idle;
    else
        state_next <= idle;
    else
        state_next <= op;
    end if;</pre>
```

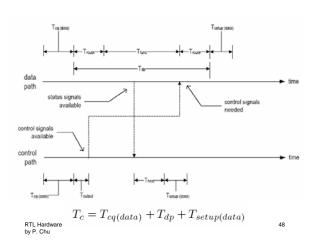
# 5. Clock rate and Performance of FSMD

- · Maximal clock rate
  - More difficult to analyze because of two interactive loops
  - The boundary of the clock rate can be found

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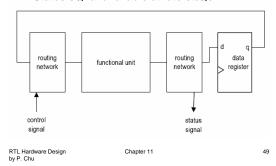
- Best-case scenario:
  - Control signals needed at late stage
  - Status signal available at early stage

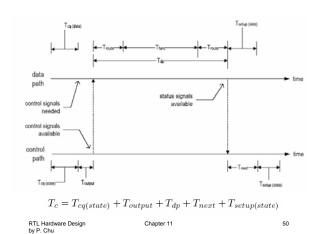




#### • Best-case scenario:

- Control signals needed at early stage
- Status signal available at late stage





 $T_{cq} + T_{dp} + T_{setup} \le T_c \le T_{cq} + T_{output} + T_{dp} + T_{next} + T_{setup}$ 

$$\frac{1}{T_{cq} + T_{output} + T_{dp} + T_{next} + T_{setup}} \leq f \leq \frac{1}{T_{cq} + T_{dp} + T_{setup}}$$

· Performance of FSMD

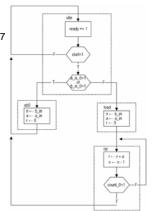
- Tc: Clock period
- K: # clock cycles to compete the computation
- Total time = K \* Tc
- K determined by algorithm, input patterns etc.

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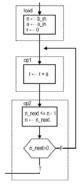
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- 8-bit input
  - Best: b=0, K=2
- Worst: b=255, K=257
- N-bit input:
  - Worst:  $K = 2+(2^n-1)$

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- 8-bit input
  - Best: b=0, K=2
  - Worst: b=255,K=2 + 255\*2
- N-bit input:
  - Worst: K=2+2\*(2<sup>n</sup>-1)



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### 6. Sequential add-and-shift multiplier

×					$a_3$ $b_3$	$a_2$ $b_2$	$a_1$ $b_1$	$a_0$ $b_0$	multiplicand multiplier
+		$a_3b_3$	$a_3b_2 \\ a_2b_3$	$a_3b_1 \\ a_2b_2 \\ a_1b_3$	$a_3b_0 \\ a_2b_1 \\ a_1b_2 \\ a_0b_3$	$a_2b_0 \\ a_1b_1 \\ a_0b_2$	$a_1b_0 \\ a_0b_1$	$a_0b_0$	
	$y_7$	$y_6$	$y_5$	$y_4$	$y_3$	$y_2$	$y_1$	$y_0$	product

 $a = a_in;$ 

 $b = b_in;$ 

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a = a\_in;

b = b\_in;

n = 8;

```
n = 8;
p = 0;
p = 0;
while (n!=0) {
                                   if b(0)=1 then {
                            op:
   if (b(0)=1) then {
                                      p = p + a;}
a = a << 1;
      p = p + a;
   a = a << 1;
b = b >> 1;
                                      b = b >> 1;
                                   n = n-1
   n = n-1; 
                                   if (n !=0) then {
return(p);
                                       goto op;}
                                   return(p);
```

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```
architecture shift_add_raw_arch of seq_mult is
  constant WIDTH: integer:=8;
    constant C_WIDTH: integer:=4; — width of the counter constant C_INIT: unsigned(C_WIDTH-1 downto 0):="1000";
     type state_type is (idle, add, shift);
    signal state_reg, state_next: state_type;
signal b_reg, b_next: unsigned(WIDTH-1 downto 0);
signal a_reg, a_next: unsigned(2*WIDTH-1 downto 0);
    signal n_reg, n_next: unsigned(C_WIDTH-1 downto 0);
    signal p_reg, p_next: unsigned(2*WIDTH-1 downto 0);
```

```
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                                                                                                           59
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```

1. Multiply the digits of the multiplier  $(b_3, b_2, b_1 \text{ and } b_0)$  by the multiplicand (A) one at a time to obtain  $b_3 * A$ ,  $b_2 * A$ ,  $b_1 * A$  and  $b_0 * A$ . The  $b_i * A$  operation is bitwise and operations of  $b_i$  and the digits of A:

```
b_i * A = (a_3 \cdot b_i, a_2 \cdot b_i, a_1 \cdot b_i, a_0 \cdot b_i)
```

- 2. Shift b<sub>i</sub> \* A to the left by i positions according to the position of digits b<sub>i</sub>.
- Add the shifted b<sub>i</sub> \* A to obtain the final product.

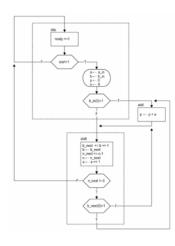
```
n = 0;
p = 0;
while (n!=8) {
   if (b_in(n)=1) then{
     p = p + (a_in << n);}
  n = n+1:
}
return (p);
```

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```
· Note the use of
  b next and n next
```

- a<<1 and b>>1 require no logic
- 8-bit input
  - Best: b=0, K = 1 + 8
  - Worst: b=255. K = 1 + 8\*2
- N-bit input:
  - Worst: K=2+2\*n

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```
combinational circuit
                          process(start, state_reg, b_reg, a_reg, n_reg, p_reg, b_in, a_in, n_next) begin
                                   b_next <= b_reg;
                                   a_next <= a_reg;
a_next <= a_reg;
n_next <= n_reg;
p_next <= p_reg;
ready <= '0';
                                   ready <='0';
case state_rog is
when idle =>
    if start-'1' then
        b_next <= unsigned(b_in);
        a_next <= "00000000" & uneigned(a_in);
        n_next <= C_INIT;
        p_next <= (others=>'0');
    if b_in(0)='1' then
        state_next <= add;
else</pre>
                                                            state_next <= add;
else
    state_next <= shift;
end if;</pre>
                                           state_next <- idle;
end if;
ready <-'1';
when add =>
                                                    p_next <= p_reg + a_reg;
state_next <- shift;
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                                                                                                                                                                              60
```

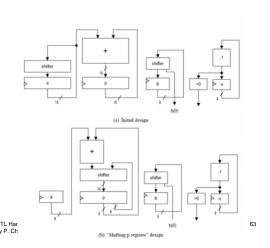
#### • Refinement

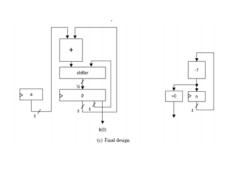
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RTL Hardware Design by P. Chu

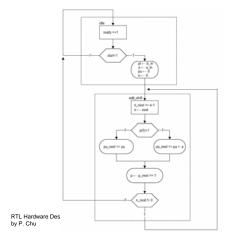
- No major computation done in the shift state: the add and shift states can be merged
- Data path can be simplified:
  - Replace 2n-bit adder with (n+1)-bit adder
  - Reduce the a register from 2n bits to n bits
  - Use the lower part of the p register to store B and eliminate the b register

Chapter 11





Chapter 11



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Design method	# Clock cycles	Size of functional units	# Register bits	
Repetitive-addition	$2 \text{ to } 2^n + 1$	2n-bit adder, n-bit decrementor	4n	
Add-and-shift (original)	n + 1 to $2n + 1$	$2n$ -bit adder, $\lceil \log_2(n+1) \rceil$ -bit dec	$5n + \lceil \log_2(n+1) \rceil$	
Add-and-shift (refined)	n+1	n-bit adder, $\lceil \log_2(n+1) \rceil$ -bit dec	$3n + \lceil \log_2(n+1) \rceil + 1$	

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