

COEN 6501 Digital design and Synthesis

Oct. 18, 2010

Lecturer: Asim J. Al-Khalili

Answer all Questions. All Questions carry equal marks

Exam Duration: 1hr 30 min.

No books, papers or calculators are allowed.

Question 1

Design a circuit to give F

$F = X^3$ where X is a 2-bit unsigned binary number, ie $X = x_1 x_0$

- a) Use Truth Table
- b) Use carry Save Adders

Question 2

a) Using Booth Algorithm multiply $A = -23$ and $B = 6$.

b) Using a 3 to 8 decoder map (recode) the
3 bits of the multiplicand according to the following equation:

$$Z_i = -2x_{i+1} + x_i + x_{i-1}$$

(ie 3 bit input $-2x_{i+1}, x_i, x_{i-1}$ giving 5 bit output $+, -, 0, 1, 2$)

Question 3

- a) Use Carry Select adder to implement optimally the addition of two 21 bit unsigned numbers.
- b) How does that compare with Manchester Carry Adder of the same size ?
Calculate the delay and area in terms of Half Adders, Full adders, gates and Muxes.

Q1 $F = \boxed{x_1}^3$

CSEV6501 - Oct - 1.0

1/3

a) Using Truth Table max value of $F = (11)^3 = 27$

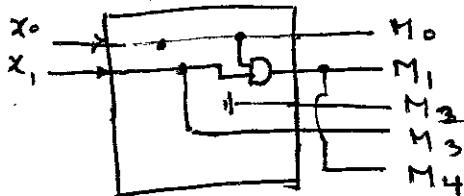
x_1, x_0	M ₄	M ₃	M ₂	M ₁	M ₀
0 0	0	0	0	0	0
0 1	0	0	0	0	1
1 0	0	1	0	0	0
1 1	1	1	1	1	1

$$M_0 = x_0$$

$$M_1 = x_1 x_0$$

$$M_2 = 0$$

$$M_3 = x_1, \quad M_4 = x_1 x_0$$

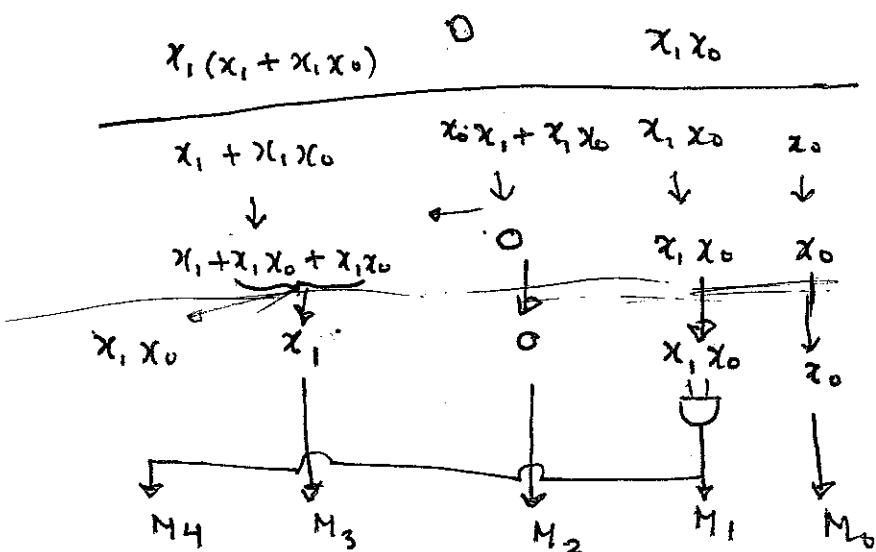


b) Using CSA method

$$\begin{array}{r}
 x_1, x_0 \\
 x_1, x_0 \\
 \hline
 x_1, x_0 \quad x_0, x_0
 \end{array}$$

$$\begin{array}{r}
 x_1, x_1 \quad x_1, x_0 \\
 \hline
 x_1 + x_1 x_0 \quad 0 \quad x_0 \\
 x_1, x_0 \quad \leftarrow X
 \end{array}
 = X^2$$

$$\begin{array}{r}
 x_0 (x_1 + x_1 x_0) \quad \textcircled{1} \quad x_0 \quad x_0 \\
 \hline
 \end{array}$$



Q2

COEN6501 - Oct-10

P2/3

$$A = (-23)_{10}$$

$$A = 0010111$$

$$- A = 1101001$$

$$B = 0000110$$

$$A * B$$

$$= \begin{array}{r} 11101001 \\ 000\cancel{0}\overset{2}{\cancel{0}}\overset{1}{1}\overset{0}{0} \\ \hline -2 \end{array}$$

Code (0 2 -2)

$$\text{Then } A * B =$$

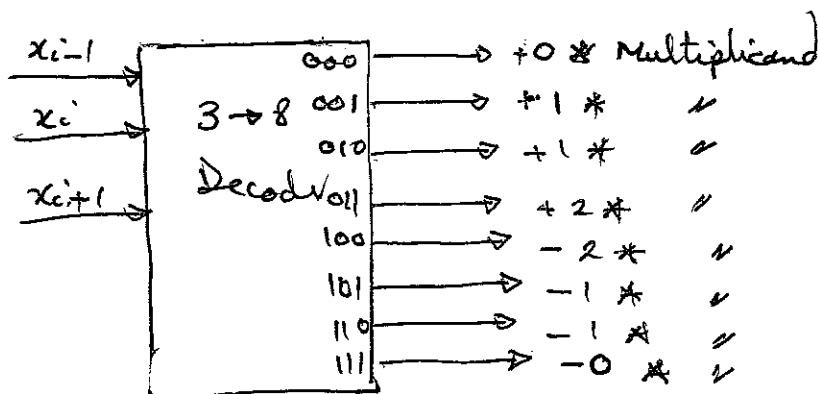
$$\begin{array}{r} 11101001 \\ 0 \quad 2 \quad -2 \\ \hline 000010110 \\ 11010010 \\ \hline 11101110110 \end{array}$$

$A * B$ is a -ve number taking its complement gives

$$00010001010_2 \text{ or } -138_{10}$$

b)

$$z_i = -2x_{i+1} + x_i + x_{i-1}$$



Q3

COGN6501 - Oct - 10

P3/3

Carry Select

Various options of implementation is possible, here are some possibilities

$$2+2+2+2+2+2+2+2+2+3 \rightarrow 3 + 7 \times \frac{1}{2} = 6\frac{1}{2} \text{ CFA}$$

$$3+3+3+3+3+3+3 \rightarrow 3 \text{ CFA} + 6 \times \frac{1}{2} \text{ CFA} = 6 \text{ CFA} \rightarrow \text{Optimal}$$

$$4+4+4+4+5$$

$$5 \text{ CFA} + 2 \times \frac{1}{2} \text{ CFA} = 6 \text{ CFA} \rightarrow \text{Optimal}$$

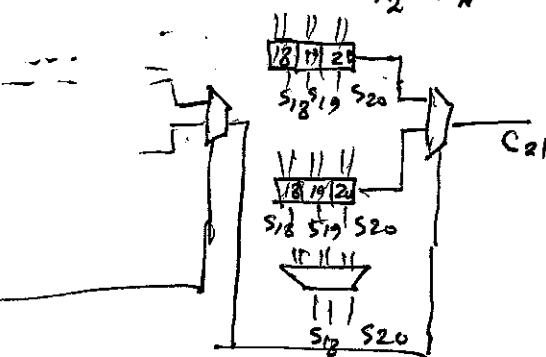
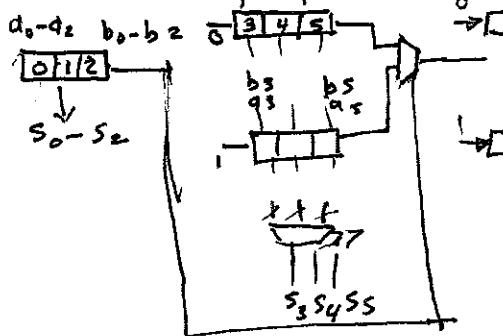
$$5+5+5+6$$

$$6 \text{ CFA} + \frac{1}{2} \text{ CFA} = 6\frac{1}{2}$$

$$3+6+6+6$$

$$6 \text{ CFA} + 3 \frac{1}{2} \text{ CFA} = 7\frac{1}{2} \text{ CFA}$$

$$\begin{matrix} b_3 \\ b_2 \\ b_1 \\ b_0 \end{matrix} \quad \begin{matrix} q_3 \\ q_2 \\ q_1 \\ q_0 \end{matrix} \quad \begin{matrix} M \\ M \\ M \\ M \end{matrix}$$

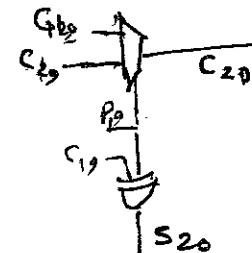
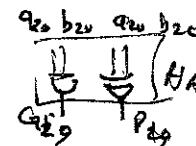
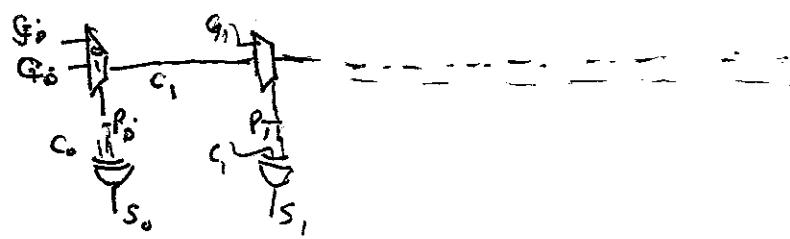
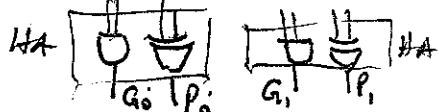


$$\text{Delay} = 3 \text{ CFA} + 6 \times \frac{1}{2} \text{ CFA} = 6 \text{ CFA}$$

$$\text{Area} = 3 \times 13 A_{\text{FA}} + (6 \times 3 + 6) A_{\text{MUX}}$$

Manchester Carry

a₀, b₀, a₁, b₁



$$\text{Delay} = \text{C}_H A + 2 \text{ C}_Mux + \text{C}_XOR$$

$$\text{Area} = 21 A_{\text{HA}} + 2 \text{ C}_Mux + 2 \text{ C}_MAX$$

Area wise Manchester carry outperforms carry select Adder

Speed wise Carry Select Adder outperforms Manchester carry Adder